

Principales dérivées et différentielles

Fonctions	Dérivées	Différentielles
$y = \frac{1}{x}$	$y' = -\frac{1}{x^2}$	$dy = -\frac{dx}{x^2}$
$y = \frac{1}{u}$	$y' = -\frac{u'}{u^2}$	$y' = -\frac{du}{u^2} = -\frac{u' dx}{u^2}$
$y = \sqrt{x}$	$y' = \frac{1}{2\sqrt{x}}$	$dy = \frac{dx}{2\sqrt{x}}$
$y = \sqrt{u}$	$y' = \frac{u'}{2\sqrt{u}}$	$dy = \frac{du}{2\sqrt{u}} = \frac{u' dx}{2\sqrt{u}}$
$y = x^n$	$\frac{dy}{dx} = y'(x) = nx^{n-1}$	$dy = nx^{n-1} dx$
$y = u^n$ avec $u = f(x)$	$y'(x) = nu^{n-1} u'$	$dy = nu^{n-1} u' dx$
$y = uv$ Avec $u = f(x)$ et $v = g(x)$	$y'(x) = u'v + uv'$	$dy = vu' dx + uv' dx$ ou $dy = v du + u dv$
$y = \frac{u}{v}$	$y'(x) = \frac{u'v - uv'}{v^2}$	$dy = \frac{1}{v^2} (vu' dx - uv' dx)$ ou $dy = \frac{1}{v^2} (v du - u dv)$
$y = e^x$	$y'(x) = e^x$	$dy = e^x dx$
$y = e^u$	$y'(x) = u' e^u$	$dy = u' e^u dx$
$y = e^{uv}$	$y'(x) = (u'v + uv') e^{uv}$	$dy = (vu' dx + uv' dx) e^{uv}$ ou $dy = (v du + u dv) e^{uv}$
$y = \ln x$	$y'(x) = \frac{1}{x}$	$dy = \frac{dx}{x}$
$y = \ln u$	$y'(x) = \frac{u'}{u}$	$dy = \frac{u'}{u} dx = \frac{du}{u}$
$y = \ln(uv)$	$y'(x) = \frac{u'}{u} + \frac{v'}{v}$	$dy = \frac{u'}{u} dx + \frac{v'}{v} dx$ ou $dy = \frac{du}{u} + \frac{dv}{v}$
$y = \ln \frac{u}{v}$	$y'(x) = \frac{u'}{u} - \frac{v'}{v}$	$dy = \frac{u'}{u} dx - \frac{v'}{v} dx$ ou $dy = \frac{du}{u} - \frac{dv}{v}$
$y = \sin x$	$y'(x) = \cos x$	$dy = \cos x dx$
$y = \sin u$	$y'(x) = u' \cos u$	$dy = u' \cos u dx = \cos u du$
$y = \cos x$	$y'(x) = -\sin x$	$dy = -\sin x dx$
$y = \cos u$	$y'(x) = -u' \sin u$	$dy = -u' \sin u dx = -\sin u du$
$y = (\sin u)^n$	$y'(x) = nu' (\sin u)^{n-1} \cos u$	$dy = nu' (\sin u)^{n-1} \cos u dx$
$y = (\cos u)^n$	$y'(x) = -nu' (\cos u)^{n-1} \sin u$	$dy = -nu' (\cos u)^{n-1} \sin u dx$
$y = \tan x$	$y'(x) = \frac{1}{\cos^2 x} = 1 + \tan^2 x$	$dy = \frac{dx}{\cos^2 x} = (1 + \tan^2 x) dx$
$y = \tan u$	$y'(x) = \frac{u'}{\cos^2 u} = u' (1 + \tan^2 u)$	$dy = \frac{u' dx}{\cos^2 u} = u' (1 + \tan^2 u) dx$ ou $dy = \frac{du}{\cos^2 u} = (1 + \tan^2 u) du$